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Chapter 8 EXERGY: A MEASURE OF WORK POTENTIAL

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Objectives

- Examine the performance of engineering devices in light of the second law of thermodynamics.
- Define *exergy*, which is the maximum useful work that could be obtained from the system at a given state in a specified environment.
- Define reversible work, which is the maximum useful work that can be obtained as a system undergoes a process between two specified states.
- Define the exergy destruction, which is the wasted work potential during a process as a result of irreversibilities.
- Define the second-law efficiency.
- Develop the exergy balance relation.
- Apply exergy balance to closed systems and control volumes.

EXERGY: WORK POTENTIAL OF ENERGY

The useful work potential of a given amount of energy at some specified state is called *exergy*, which is also called the *availability* or *available energy*.

A system is said to be in the dead state when it is in thermodynamic equilibrium with the environment it is in.



At the dead state, the useful work potential (exergy) of a system is zero.

A system that is in equilibrium with its environment is said to be at the dead state. A system delivers the maximum possible work as it undergoes a reversible process from the specified initial state to the state of its environment, that is, the dead state.

This represents the *useful work potential* of the system at the specified state and is called exergy.

Exergy represents the upper limit on the amount of work a device can deliver without violating any thermodynamic laws.



The immediate surroundings of a hot potato are simply the temperature gradient zone of the air next to the potato.



The atmosphere contains a tremendous amount of energy, but no exergy.

Exergy (Work Potential) Associated with Kinetic and Potential Energy

Exergy of kinetic energy:

 $x_{\rm pe} = {\rm pe} = gz$ (kJ/kg)

Exergy of potential energy:

 $x_{\rm ke} = {\rm ke} = {V^2 \over 2}$ (The exergies of kinetic and potential energies are equal to themselves, and

they are entirely available for work.

(kJ/kg) The work potential or exergy of potential energy is equal to the potential energy itself.



Unavailable energy is the portion of energy that cannot be converted to work by even a reversible heat engine.

REVERSIBLE WORK AND IRREVERSIBILITY



SECOND-LAW EFFICIENCY, $\eta_{||}$



device relative to its performance

under reversible conditions.

Two heat engines that have the same thermal efficiency, but different maximum thermal efficiencies.

Sink

300 K

Source

1000 K

B

 $\eta_{\rm th} = 30\%$

 $\eta_{\rm th,max} = 70\%$



Second-law efficiency of all reversible devices is 100%.

EXERGY CHANGE OF A SYSTEM

Exergy of a Fixed Mass: Nonflow (or Closed System) Exergy

$$\underbrace{\delta E_{\text{in}} - \delta E_{\text{out}}}_{\text{Net energy transfer}} = \underbrace{dE_{\text{system}}}_{\text{Change in internal, kinetic}} \\ - \delta Q - \delta W = dU$$

$$\delta W = P \, dV = (P - P_0) \, dV + P_0 \, dV = \delta W_{b,\text{useful}} + P_0 \, dV$$

$$\delta W_{\rm HE} = \left(1 - \frac{T_0}{T}\right) \delta Q = \delta Q - \frac{T_0}{T} \delta Q = \delta Q - (-T_0 \, dS) \rightarrow \delta Q = \delta W_{\rm HE} - T_0 \, dS$$

$$\delta W_{\text{total useful}} = \delta W_{\text{HE}} + \delta W_{b,\text{useful}} = -dU - P_0 \, dV + T_0 \, dS$$

$$X = (U - U_0) + P_0(V - V_0) - T_0(S - S_0) + m\frac{V^2}{2} + mgz$$

Exergy of a closed system



The *exergy* of a specified mass at a specified state is the useful work that can be produced as the mass undergoes a reversible process to the state of the environment.



Exergy of a Flow Stream: Flow (or Stream) Exergy

$$x_{\text{flowing fluid}} = x_{\text{nonflowing fluid}} + x_{\text{flow}}$$

$$= (u - u_0) + P_0(v - v_0) - T_0(s - s_0) + \frac{V^2}{2} + gz + (P - P_0)v$$

$$= (u + Pv) - (u_0 + P_0v_0) - T_0(s - s_0) + \frac{V^2}{2} + gz$$

$$= (h - h_0) - T_0(s - s_0) + \frac{V^2}{2} + gz$$

$$Flow$$

$$exergy$$

$$\psi = (h - h_0) - T_0(s - s_0) + \frac{V^2}{2} + gz$$
Exergy change of flow
$$\Delta \psi = \psi_2 - \psi_1 = (h_2 - h_1) + T_0(s_2 - s_1) + \frac{V_2^2 - V_1^2}{2} + g(z_2 - z_1)$$

$$The exergy$$

$$associated with$$

$$fluid downstream$$

$$Flowing$$

$$P_0$$

$$V = P_0v + w_{shaft}$$

$$Flow$$

$$Pv = P_0v + w_{shaft}$$

$$Flow$$

$$Pv = P_0v + w_{shaft}$$

$$Flow$$

$$Pv = P_0v + w_{shaft}$$

$$Flow$$

$$Flow$$

$$Pv = P_0v + w_{shaft}$$

$$Flow$$

Energy:

$$e = u + \frac{V^2}{2} + gz$$
Fixed
mass
Exergy:
 $\phi = (u - u_0) + P_0(v - v_0) - T_0(s - s_0) + \frac{V^2}{2} + gz$
(a) A fixed mass (nonflowing)

Energy:

$$\theta = h + \frac{V^2}{2} + gz$$
Fluid
stream

Exergy:
 $\psi = (h - h_0) + T_0(s - s_0) + \frac{V^2}{2} + gz$
(b) A fluid stream (flowing)

The *energy* and *exergy* contents of (*a*) a fixed mass (*b*) a fluid stream.



fraction of the energy transferred from a heat source at temperature T that can be converted to work in an environment at temperature T_0 .

T₂

 $\frac{Q}{T_2}$

Exergy Transfer by Work, W

 $W_{\rm surr} = P_0(V_2 - V_1)$

 $X_{\text{work}} = \begin{cases} W - W_{\text{surr}} & \text{(for boundary work)} \\ W & \text{(for other forms of work)} \end{cases}$

Exergy Transfer by Mass, *m*

$$X_{\text{mass}} = m\psi$$
 $\psi = (h - h_0) - T_0(s - s_0) + \frac{V^2}{2} + gz$

$$\dot{X}_{\text{mass}} = \int_{A_c} \psi \rho V_n \, dA_c \qquad X_{\text{mass}} = \int \psi \, \delta m = \int_{\Delta t} \dot{X}_{\text{mass}} \, dt$$





There is no useful work transfer associated with boundary work when the pressure of the system is maintained constant at atmospheric pressure.

Mass contains energy, entropy, and exergy, and thus mass flow into or out of a system is accompanied by energy, entropy, and exergy transfer.

THE DECREASE OF EXERGY PRINCIPLEAND EXERGY DESTRUCTIONNo heat, work

Energy balance:

$$E_{\text{in}}^{\not \to 0} - E_{\text{out}}^{\not \to 0} = \Delta E_{\text{system}} \rightarrow 0 = E_2 - E_1$$

Entropy balance:

$$S_{\text{in}}^{\nearrow 0} - S_{\text{out}}^{\nearrow 0} + S_{\text{gen}} = \Delta S_{\text{system}} \rightarrow S_{\text{gen}} = S_2 - S_1$$

Multiplying the second relation by T_0 and subtracting it from the first one gives

$$-T_0 S_{\text{gen}} = E_2 - E_1 - T_0 (S_2 - S_1)$$
(8–29)

From Eq. 8–17 we have

$$X_{2} - X_{1} = (E_{2} - E_{1}) + P_{0}(V_{2} - V_{1})^{\nearrow 0} - T_{0}(S_{2} - S_{1})$$

$$= (E_{2} - E_{1}) - T_{0}(S_{2} - S_{1})$$
(8-30)

since $V_2 = V_1$ for an isolated system (it cannot involve any moving boundary and thus any boundary work). Combining Eqs. 8–29 and 8–30 gives

$$-T_0 S_{\text{gen}} = X_2 - X_1 \le 0 \tag{8-31}$$

since T_0 is the thermodynamic temperature of the environment and thus a positive quantity, $S_{\text{gen}} \ge 0$, and thus $T_0 S_{\text{gen}} \ge 0$. Then we conclude that

$$\Delta X_{\text{isolated}} = (X_2 - X_1)_{\text{isolated}} \le 0$$

No heat, work
or mass transfer
Isolated system
$$\Delta X_{\text{isolated}} \leq 0$$

(or $X_{\text{destroyed}} \geq 0$)

The isolated system considered in the development of the decrease of exergy principle.

The exergy of an isolated system during a process always decreases or, in the limiting case of a reversible process, remains constant. In other words, it never increases and exergy is destroyed during an actual process. This is known as the decrease of exergy principle.

(8 - 32)

Exergy Destruction

 $X_{\text{destroyed}} = T_0 S_{\text{gen}} \ge 0$

$X_{\text{destroyed}}$	(>0	Irreversible process
	= 0	Reversible process
	$\langle 0 \rangle$	Impossible process

Exergy destroyed is a *positive quantity* for any actual process and becomes *zero* for a reversible process.

Exergy destroyed represents the lost work potential and is also called the *irreversibility* or *lost work*.

Can the exergy change of a system during a process be negative?



The exergy change of a system can be negative, but the exergy destruction cannot.

Consider heat transfer from a system to its surroundings. How do you compare exergy changes of the system and the surroundings?

EXERGY BALANCE: CLOSED SYSTEMS



Closed system:
$$X_{\text{heat}} - X_{\text{work}} - X_{\text{destroyed}} = \Delta X_{\text{system}}$$

Closed system:
$$\sum \left(1 - \frac{T_0}{T_k}\right)Q_k - \left[W - P_0(V_2 - V_1)\right] - T_0S_{gen} = X_2 - X_2$$

Rate form:
$$\sum \left(1 - \frac{T_0}{T_k}\right)\dot{Q}_k - \left(\dot{W} - P_0\frac{dV_{\text{system}}}{dt}\right) - T_0\dot{S}_{\text{gen}} = \frac{dX_{\text{system}}}{dt}$$

The heat transfer to a system and work done by the system are taken to be positive quantities.

 Q_k is the heat transfer through the boundary at temperature T_k at location k.



EXAMPLES

Exergy balance for heat conduction

$$\underbrace{\dot{X}_{\text{in}} - \dot{X}_{\text{out}}}_{\text{Rate of net exergy transfer}} - \underbrace{\dot{X}_{\text{destroyed}}}_{\text{Rate of exergy}} = \underbrace{dX_{\text{system}}/dt}_{\text{Rate of change}} = 0$$
Rate of net exergy transfer destruction in exergy

$$\dot{Q}\left(1 - \frac{T_0}{T}\right)_{\rm in} - \dot{Q}\left(1 - \frac{T_0}{T}\right)_{\rm out} - \dot{X}_{\rm destroyed} = 0$$



Exergy balance for expansion of steam





EXERGY BALANCE: CONTROL VOLUMES

$$X_{\text{heat}} - X_{\text{work}} + X_{\text{mass,in}} - X_{\text{mass,out}} - X_{\text{destroyed}} = (X_2 - X_1)_{\text{CV}}$$

$$\sum \left(1 - \frac{T_0}{T_k}\right) Q_k - \left[W - P_0(V_2 - V_1)\right] + \sum_{\text{in}} m\psi - \sum_{\text{out}} m\psi - X_{\text{destroyed}} = (X_2 - X_1)_{\text{CV}}$$

$$\sum \left(1 - \frac{T_0}{T_k}\right) \dot{Q}_k - \left(\dot{W} - P_0 \frac{dV_{\rm CV}}{dt}\right) + \sum_{\rm in} \dot{m}\psi - \sum_{\rm out} \dot{m}\psi - \dot{X}_{\rm destroyed} = \frac{dX_{\rm CV}}{dt}$$

The rate of exergy change within the control volume during a process is equal to the rate of net exergy transfer through the control volume boundary by heat, work, and mass flow minus the rate of exergy destruction within the boundaries of the control volume.



Exergy is transferred into or out of a control volume by mass as well as heat and work transfer.

Exergy Balance for Steady-Flow Systems

Most control volumes encountered in practice such as turbines, compressors, nozzles, diffusers, heat exchangers, pipes, and ducts operate steadily, and thus they experience no changes in their mass, energy, entropy, and exergy contents as well as their volumes. Therefore, $dV_{CV}/dt = 0$ and $dX_{CV}/dt = 0$ for such systems.



Reversible Work, W_{rev}

The exergy balance relations presented above can be used to determine the reversible work W_{rev} by setting the exergy destroyed equal to zero. The work W in that case becomes the reversible work.

General: $W = W_{rev}$ when $X_{destroyed} = 0$ Single stream: $\dot{W}_{rev} = \dot{m}(\psi_1 - \psi_2) + \sum \left(1 - \frac{T_0}{T_k}\right)\dot{Q}_k$ (kW)Adiabatic, single stream: $\dot{W}_{rev} = \dot{m}(\psi_1 - \psi_2)$

The exergy destroyed is zero only for a reversible process, and reversible work represents the maximum work output for workproducing devices such as turbines and the minimum work input for work-consuming devices such as compressors.

Second-Law Efficiency of Steady-Flow Devices, $\eta_{||}$

The second-law efficiency of various steady-flow devices can be determined from its general definition, $\eta_{II} = (Exergy recovered)/(Exergy supplied)$. When the changes in kinetic and potential energies are negligible and the devices are adiabatic:

$$\eta_{\text{II,turb}} = \frac{w}{w_{\text{rev}}} = \frac{h_1 - h_2}{\psi_1 - \psi_2} \quad \text{or} \quad \eta_{\text{II,turb}} = 1 - \frac{T_0 s_{\text{gen}}}{\psi_1 - \psi_2} \quad \text{Turbine}$$

$$\eta_{\text{II,comp}} = \frac{w_{\text{rev,in}}}{w_{\text{in}}} = \frac{\psi_2 - \psi_1}{h_2 - h_1} \quad \text{or} \quad \eta_{\text{II,comp}} = 1 - \frac{T_0 s_{\text{gen}}}{h_2 - h_1} \quad \text{Compressor}$$

$$\eta_{\text{II,HX}} = \frac{\dot{m}_{\text{cold}}(\psi_4 - \psi_3)}{\dot{m}_{\text{hot}}(\psi_1 - \psi_2)} \quad \text{Heat}_{\text{exchanger}}$$

$$\eta_{\text{II,HX}} = 1 - \frac{T_0 \dot{s}_{\text{gen}}}{\dot{m}_{\text{hot}}(\psi_1 - \psi_2)} \quad \text{Heat}_{\text{exchanger}}$$

$$\eta_{\text{II,HX}} = \frac{\dot{m}_{3}\psi_3}{\dot{m}_{1}\psi_1 + \dot{m}_2\psi_2} \quad \text{Mixing}_{\text{chamber}}$$

$$\eta_{\text{II,mix}} = \frac{\dot{m}_3\psi_3}{\dot{m}_1\psi_1 + \dot{m}_2\psi_2} \quad \text{Mixing}_{\text{chamber}}$$

$$\eta_{\text{II,mix}} = 1 - \frac{T_0 \dot{s}_{\text{gen}}}{\dot{m}_1\psi_1 + \dot{m}_2\psi_2} \quad \dot{s}_{\text{gen}} = \dot{m}_3s_3 - \dot{m}_2s_2 - \dot{m}_1s_1$$



$$W_{\text{rev,in}} + m_1 \psi_1^{\neq 0} = m_2 \phi_2 - m_1 \phi_1^{\neq 0}$$

 $W_{\text{rev,in}} = m_2 \phi_2$



Summary

• Exergy: Work potential of energy

✓ Exergy (work potential) associated with kinetic and potential energy

- Reversible work and irreversibility
- Second-law efficiency
- Exergy change of a system
 - ✓ Exergy of a fixed mass: Nonflow (or closed system) exergy
 - ✓ Exergy of a flow stream: Flow (or stream) exergy
- Exergy transfer by heat, work, and mass
- The decrease of exergy principle and exergy destruction
- Exergy balance: Closed systems
- Exergy balance: Control volumes
 - Exergy balance for steady-flow systems
 - ✓ Reversible work
 - ✓ Second-law efficiency of steady-flow devices